Geometrical reasoning: lines, angles and shapes

As outcomes, Year 8 pupils should, for example:

Know and use side, angle and symmetry properties of equilateral, isosceles and right-angled triangles.

For example:

- Discuss whether it is possible to draw or construct on a 3 by 3 pinboard:
 - a. a triangle with a reflex angle;
 - b. an isosceles trapezium;
 - c. an equilateral triangle or a (non-square) rhombus.

If not, explain why not.

Classify quadrilaterals by their geometric properties

(equal and/or parallel sides, equal angles, right angles, diagonals bisected and/or at right angles, reflection and rotation symmetry...).

Know properties such as:

- An isosceles trapezium is a trapezium in which the two opposite non-parallel sides are the same length. It has one line of symmetry and both diagonals are the same length.
- A parallelogram has its opposite sides equal and parallel. Its diagonals bisect each other. It has rotation symmetry of order 2.
- A rhombus is a parallelogram with four equal sides. Its diagonals bisect each other at right angles. Both diagonals are lines of symmetry. It has rotation symmetry of order 2.
- A kite is a quadrilateral that has two pairs of adjacent sides of equal length, and no interior angle larger than 180°. It has one line of symmetry and its diagonals cross at right angles.
- An arrowhead or delta has two pairs of adjacent edges of equal length and one interior angle larger than 180°. It has one line of symmetry. Its diagonals cross at right angles outside the shape.

Provide a convincing argument to explain, for example, that a rhombus is a parallelogram but a parallelogram is not necessarily a rhombus.

Devise questions for a tree classification diagram to sort a given set of quadrilaterals.

 Identify then classify the 16 distinct quadrilaterals that can be constructed on a 3 by 3 pinboard.

Link to standard constructions (pages 220–3).

As outcomes, Year 9 pupils should, for example:

Know and use angle and symmetry properties of polygons, and angle properties of parallel and intersecting lines, to solve problems and explain reasoning. For example:

 Deduce the angles of the rhombus in this arrangement of three identical tiles.



What can you deduce about the shape formed by the outline?

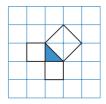
- Explain why:
 - Equilateral triangles, squares and regular hexagons will tessellate on their own but other regular polygons will not.
 - Squares and regular octagons will tessellate together.

Know and use properties of triangles, including Pythagoras' theorem.

Know that:

- In any triangle, the largest angle is opposite the longest side and the smallest angle is opposite the shortest side.
- In a right-angled triangle, the side opposite the right angle is the longest and is called the hypotenuse.

Understand, recall and use Pythagoras' theorem. Explain special cases of Pythagoras' theorem in geometrical arrangements such as:



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