

NUMBERS AND THE NUMBER SYSTEM

Pupils should be taught to:

Understand and use decimal notation and place value; multiply and divide integers and decimals by powers of 10 (continued)

As outcomes, Year 7 pupils should, for example:

Multiply and divide numbers by 10, 100 and 1000.

Investigate, describe the effects of, and explain multiplying and dividing a number by 10, 100, 1000, e.g. using a place value board, **calculator** or **spreadsheet**.

In particular, recognise that:

- Multiplying a positive number by 10, 100, 1000... has the effect of increasing the value of that number.
- Dividing a positive number by 10, 100, 1000... has the effect of decreasing the value of that number.
- When a number is multiplied by 10, the digits move one place to the left:

$$\begin{array}{r} 34.12 \\ \times 10 \\ \hline 341.2 \end{array} \quad 34.12 \text{ multiplied by } 10 = 341.2$$

- When a number is divided by 10, the digits move one place to the right:

$$\begin{array}{r} 34.1 \\ \div 10 \\ \hline 3.41 \end{array} \quad 34.1 \text{ divided by } 10 = 3.41$$

Complete statements such as:

$$\begin{array}{ll} 4 \times 10 = \square & 4 \times \square = 400 \\ 4 \div 10 = \square & 4 \div \square = 0.04 \\ 0.4 \times 10 = \square & 0.4 \times \square = 400 \\ 0.4 \div 10 = \square & 0.4 \div \square = 0.004 \\ \square \div 100 = 0.04 & \square \div 10 = 40 \\ \square \times 1000 = 40\,000 & \square \times 10 = 400 \end{array}$$

See Y456 examples (pages 6–7).

[Link to converting mm to cm and m, cm to m, m to km...](#)
(pages 228–9).

As outcomes, Year 8 pupils should, for example:

Multiply and divide numbers by 0.1 and 0.01.

Investigate, describe the effects of, and explain multiplying and dividing a number by 0.1 and 0.01, e.g. using a **calculator** or **spreadsheet**.

In particular, recognise how numbers are increased or decreased by these operations.

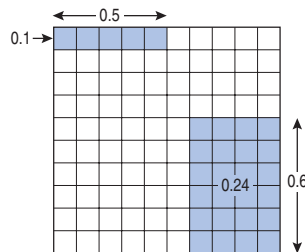
0.1 is equivalent to $\frac{1}{10}$ and 0.01 is equivalent to $\frac{1}{100}$, so:

- **Multiplying by 0.1** has the same effect as multiplying by $\frac{1}{10}$ or dividing by 10. For example, 3×0.1 has the same value as $3 \times \frac{1}{10}$, which has the same value as $3 \div 10 = 0.3$, and 0.3×0.1 has the same value as $\frac{3}{10} \times \frac{1}{10} = \frac{3}{100} = 0.03$.
- **Multiplying by 0.01** has the same effect as multiplying by $\frac{1}{100}$ or dividing by 100. For example, 3×0.01 has the same value as $3 \times \frac{1}{100}$, which has the same value as $3 \div 100 = 0.03$, and 0.3×0.01 has the same value as $\frac{3}{10} \times \frac{1}{100} = \frac{3}{1000} = 0.003$.
- **Dividing by 0.1** has the same effect as dividing by $\frac{1}{10}$ or multiplying by 10. For example, $3 \div 0.1$ has the same value as $3 \div \frac{1}{10}$. (How many tenths in three? $3 \times 10 = 30$)
 $0.3 \div 0.1$ has the same value as $\frac{3}{10} \div \frac{1}{10}$. (How many tenths in three tenths? $0.3 \times 10 = 3$)
- **Dividing by 0.01** has the same effect as dividing by $\frac{1}{100}$ or multiplying by 100. For example, $3 \div 0.01$ has the same value as $3 \div \frac{1}{100}$. (How many hundredths in three? $3 \times 100 = 300$)
 $0.3 \div 0.01$ has the same value as $\frac{3}{10} \div \frac{1}{100}$. (How many hundredths in three tenths? $0.3 \times 100 = 30$)

Complete statements such as:

$0.5 \times 0.1 = \square$ $0.8 \times \square = 0.08$
 $0.7 \div 0.1 = \square$ $0.6 \div \square = 6$

Understand a diagrammatic explanation to show, for example, that $0.1 \times 0.5 = 0.05$, or $0.24 \div 0.6 = 0.4$.



Discuss the effects of multiplying and dividing by a number less than 1.

- Does division always make a number smaller?
- Does multiplication always make a number larger?

As outcomes, Year 9 pupils should, for example:

Multiply and divide by any integer power of 10.

For example:

- Calculate:

7.34×100	$37.4 \div 100$
46×1000	$3.7 \div 1000$
$8042 \times 10\,000$	$4982 \div 10\,000$
9.3×0.1	$0.27 \div 0.1$
0.63×0.01	$5.96 \div 0.01$

Link to converting mm² to cm², cm² to m², mm³ to cm³ and cm³ to m³ (pages 228–9).

Begin to write numbers in standard form, expressing them as

$A \times 10^n$ where $1 \leq A < 10$, and n is an integer.

For example:

$734.6 = 7.346 \times 10^2$
 $0.0063 = 6.3 \times 10^{-3}$

Know how to use the 'exp' key on a **calculator** to convert from index form.

Answer questions such as:

- Complete these. The first is done for you.
 $3 \times 10^n = 300 \times 10^{n-2}$
 $0.3 \times 10^n = 30\,000 \times \square$
 $0.3 \times 10^n = 0.0003 \times \square$
 $3 \div 10^n = 0.003 \times \square$
 $0.3 \div 10^n = 300 \times \square$
 $0.003 \div 10^n = 3 \times \square$
- Put these numbers in ascending order:
 2×10^{-2} , 3×10^{-1} , 2.5×10^{-3} , 2.9×10^{-2} , 3.2×10^{-1}
- Write these numbers in standard form:
 - The population of the UK is 57 million.
 - The dwarf pigmy goby fish weighs 0.000 14oz.
 - The shortest millipede in the world measures 0.082 inches.
 - After the Sun, the nearest star is 24800000000000 miles away.
- The probability of dying before the age of 40 is 1 in 850, or 0.00118, or 1.8×10^{-3} .

These are the risks of dying from particular causes:

smoking 10 cigarettes a day	1 in 200
road accident	1 in 8000
accident at home	1 in 260 000
railway accident	1 in 500000

Write each of these as a probability in standard form.

Link to writing numbers in standard form in science and geography.