#### NUMBERS AND THE NUMBER SYSTEM

### Pupils should be taught to:

Order, add, subtract, multiply and divide positive and negative numbers

# As outcomes, Year 7 pupils should, for example:

Use, read and write, spelling correctly: integer, positive, negative, plus, minus... and know that <sup>-</sup>6 is read as 'negative six'.

#### Order integers and position them on a number line. For example:

- Put a > or < sign between these pairs of temperatures:

  -6°C -4°C -6°C -6°C -6°C -6°C -4°C -6°C
- On a number line, mark numbers half way between two given negative numbers, or between a given positive number and a given negative number.
- Use a graphical calculator to generate ten random numbers lying between <sup>-</sup>20 and <sup>+</sup>20, then arrange them in order. For example, enter:

then keep pressing the **EXE** button.

Link to plotting coordinates in all four quadrants (pages 218-19).

# Begin to add and subtract integers.

Extend patterns such as:

$$2 + 1 = 3$$
  $-3 - 1 = -4$   
 $2 + 0 = 2$   $-3 - 0 = -3$   
 $2 + -1 = 1$   $-3 - 1 = -2$   
 $2 + -2 = 0$   $-3 - 2 = -1$   
 $2 + -3 = -1$   $-3 - 3 = 0$ 

Use negative number cards to help answer questions such as:

$$\begin{bmatrix}
 3 + 5 & = \Box \\
 \hline
 146 + 659 & = \Box \\
 \hline
 9 - 4 & = \Box \\
 \hline
 537 - 125 & = \Box
 \end{bmatrix}$$
 $\begin{bmatrix}
 13 + 25 & = \Box \\
 99 + 99 & = \Box \\
 \hline
 43 - 21 & = \Box \\
 \hline
 99 - 99 & = \Box
 \end{bmatrix}$ 

Answer open-ended questions such as:

- The answer to a question was <sup>-</sup>8. What was the question?
- The result of subtracting one integer from another is <sup>-</sup>2. What could the two integers be?
- The temperature is below freezing point.
   It falls by 10 degrees, then rises by 7 degrees.
   What could the temperature be now?

Solve simple puzzles or problems involving addition and subtraction of positive and negative numbers, such as:

• Complete this magic square.



Link to substituting positive and negative numbers in expressions and formulae (pages 138-41).

As outcomes, Year 8 pupils should, for example:

As outcomes, Year 9 pupils should, for example:

Use vocabulary from previous year.

Order positive and negative decimals.

See ordering decimals (pages 40-1).

### Add and subtract integers.

Understand that 1 add <sup>-1</sup> is zero, and use this to calculate, for example:

$$1 + 1 + \overline{\phantom{a}} + 1 + \overline{\phantom{a}} + 1 + \overline{\phantom{a}} = \square$$
  $\overline{\phantom{a}} + 1 + \overline{\phantom{a}} = \square$ 

$$3 + ^{-}3 = \square$$
  $^{-}29 + 29 = \square$   $827 + ^{-}827 = \square$   $^{-}3 + \square = 0$ 

$$62 + ^{-}51 = \square$$
  $^{-}87 + 90 = \square$   $40 + ^{-}30 + 20 + ^{-}10 = \square$   $^{-}3 + \square = 7$ 

Recognise that:

- 0 1 has the same value as (1 + 1) 1 = 1;
- 0-1 has the same value as (1+1)-1=1.

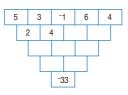
Use this to calculate, for example:

$$5 - \overline{3} = \square$$
  $\overline{4} - \overline{5} = \square$   $\overline{2} - \square = 7$ 

Use the sign change key on a **calculator** to work out:

Solve puzzles such as:

- а 19 6 7 3 -4 -8 12 | 14 | -4 b -6 -5 • Complete this table. a – b 2
- In this 'wall', subtract the right-hand from the lefthand number to find the number directly below. Fill in the empty boxes.



Link to substituting positive and negative numbers in expressions and formulae (pages 138-41).

### NUMBERS AND THE NUMBER SYSTEM

### Pupils should be taught to:

Order, add, subtract, multiply and divide positive and negative numbers (continued)

# As outcomes, Year 7 pupils should, for example:

Use positive and negative numbers in context.

For example, find:

- the final position of an object after moves forwards and backwards along a line;
- a total bank balance after money is paid in and taken out;
- the total marks in a test of 10 questions, with \*2 marks for a correct answer and \*1 mark for an incorrect answer;
- the total of scores above and below par in a round of golf;
- the mean of a set of temperatures above and below zero...

Know how to, for example:

- find the distance between two floors using a lift, including above and below ground level;
- calculate game scores which include positive and negative points;
- identify measurements above and below sea-level, using contour lines on maps;
- interpret world weather charts to find differences in temperatures around the globe;
- identify the level of accuracy in measurements, e.g. 20 cm ± 0.5cm...

Link to work in other subjects.

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# As outcomes, Year 8 pupils should, for example:

As outcomes, Year 9 pupils should, for example:

# Multiply and divide positive and negative numbers.

Link known multiplication tables to negative number multiplication tables. For example:

- $^{-}2 \times 1 = ^{-}2$ ,  $^{-}2 \times 2 = ^{-}4$ ,  $^{-}2 \times 3 = ^{-}6$  and so on ...
- Write tables, continuing the pattern:

$2 \times 2 = 4$	$2 \times ^{-}2 = ^{-}4$
$1 \times 2 = 2$	$1 \times ^{-}2 = ^{-}2$
$0 \times 2 = 0$	$0 \times ^{-}2 = 0$
$^{-}1 \times 2 = ^{-}2$	$^{-1} \times ^{-2} = 2$
$^{-}2 \times 2 = ^{-}4$	$^{-}2 \times ^{-}2 = 4$
$^{-}3 \times 2 = ^{-}6$	$^{-}3 \times ^{-}2 = 6$

Complete a multiplication table. Shade positive and negative numbers, and zero, using different colours.

Look for patterns.
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×	-3	-2	-1	0	1	2	3
3	-9	-6	-3	0	3	6	9
2	-6	-4	-2	0	2	4	6
1	-3	-2	-1	0	1	2	3
0	0	0	0	0	0	0	0
-1	3	2	1	0	-1	-2	-3
-2	6	4	2	0	-2	-4	<del>-</del> 6
-3	9	6	3	0	-3	-6	-9

Recognise that division by a negative number is the inverse of multiplication by a negative number. Use this, and the negative number multiplication tables, to show, for example, that  $^{-}4 \div ^{-}2 = 2$ , and relate this to the question 'How many '2s in '4?'

For a fact such as  $^{-}3 \times 2 = ^{-}6$ , write three other facts, i.e.  $2 \times ^{-}3 = ^{-}6$ ,  $^{-}6 \div 2 = ^{-}3$ ,  $^{-}6 \div 3 = ^{-}2$ .

Answer questions such as:

- How many negative twos make negative four?
- The answer to a question was <sup>-</sup>24.
   What was the question?

Use the sign change key on a calculator to work out:

$48 \times 53$	<sup>-</sup> 74 × 3	9.02 ÷ <sup>-</sup> 22
$68 \times ^{-}49$	$^{-}8 \times ^{-}73.7$	<sup>-</sup> 6450 ÷ <sup>-</sup> 15

Solve puzzles such as:

 Complete this multiplication grid.
 Find two ways to do it.

×		4	-9	
		-8	18	
-3		-12		
	35			-14
				12

Extend to the distributive law. For example:

$$^{-1} \times (3 + 4) = ^{-1} \times 7 = ^{-7}$$
  
 $^{-1} \times (3 + 4) = (^{-1} \times 3) + (^{-1} \times 4) = ^{-3} + ^{-4} = ^{-7}$ 

Link to substituting positive and negative numbers in expressions and formulae (page 138-41).