

Fractions, decimals, percentages, ratio and proportion

As outcomes, Year 8 pupils should, for example:

Convert decimals to fractions.

Continue to recognise that each **terminating decimal** is a fraction. For example, $0.237 = \frac{237}{1000}$.

Recognise that a **recurring decimal** is a fraction.

Convert decimals (up to three decimal places) to fractions. For example:

- Convert 0.625 to $\frac{625}{1000}$ and then cancel to $\frac{5}{8}$.

Link to percentages (pages 70–1).

Convert fractions to decimals.

Use division to convert a fraction to a decimal, without and with a calculator. For example:

- Use short division to work out that:
 $\frac{1}{5} = 0.2$ $\frac{3}{8} = 0.375$ $\frac{27}{8} = \dots$ $\frac{3}{7} = \dots$
- Use a **calculator** to work out that $\frac{7}{53} = \dots$

Investigate fractions such as $\frac{1}{3}$, $\frac{1}{6}$, $\frac{2}{3}$, $\frac{1}{6}$, $\frac{1}{11}$, ... converted to decimals. For example:

- Predict what answers you will get when you use a **calculator** to divide:
3 by 3, 4 by 3, 5 by 3, 6 by 3, and so on.

Order fractions.

Compare and order fractions by converting them to fractions with a common denominator or by converting them to decimals. For example, find the larger of $\frac{7}{8}$ and $\frac{4}{5}$:

- using common denominators:
 $\frac{7}{8}$ is $\frac{35}{40}$, $\frac{4}{5}$ is $\frac{32}{40}$, so $\frac{7}{8}$ is larger.
- using decimals:
 $\frac{7}{8}$ is 0.875, $\frac{4}{5}$ is 0.8, so $\frac{7}{8}$ is larger.

Use equivalent fractions or decimals to position fractions on a number line. For example:

- Mark fractions such as $\frac{2}{5}$, $\frac{9}{20}$, $\frac{3}{15}$, $\frac{19}{12}$ on a number line graduated in tenths, then on a line graduated in hundredths.

Answer questions such as:

- Which is greater, 0.23 or $\frac{3}{16}$?
- Which fraction is exactly half way between $\frac{3}{5}$ and $\frac{5}{7}$?

As outcomes, Year 9 pupils should, for example:

Know that a recurring decimal is an exact fraction.

Know and use simple conversions for recurring decimals to fractions. For example:

- $0.333\ 333\dots = \frac{1}{3}$ ($= \frac{3}{9}$)
- $0.666666\dots = \frac{2}{3}$
- $0.111111\dots = \frac{1}{9}$
- $0.999999\dots = \frac{9}{9} = 1$

Convert recurring decimals to fractions in simple cases, using an algebraic method. For example:

$$\begin{aligned} z &= 0.333\ 333\dots & (1) \\ 10z &= 3.333\ 333\dots & (2) \end{aligned}$$

Subtracting (1) from (2) gives:

$$\begin{aligned} 9z &= 3 \\ z &= \frac{1}{3} \end{aligned}$$

- Comment on:
 $z = 0.999\ 999\dots$
 $10z = 9.999\ 999\dots$
 $9z = 9$
 $z = 1$

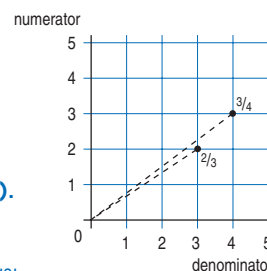
Order fractions.

Answer questions such as:

- The numbers $\frac{1}{2}$, a, b, $\frac{3}{4}$ are in increasing order of size. The differences between successive numbers are all the same. What is the value of b?
- z is a decimal with one decimal place. Write a list of its possible values, if both these conditions are satisfied:
 $\frac{1}{3} < z < \frac{2}{3}$ $\frac{1}{6} < z < \frac{5}{6}$

Link to inequalities (pages 112–13).

Order fractions by graphing them. Compare gradients.



Link to gradients (page 167–9).

Investigate sequences such as:

$$\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}, \dots, \frac{n}{n+1}$$

Investigate what happens as the sequence continues and n tends towards infinity.

Convert the fractions to decimals or draw a graph of the decimal against the term number.