As outcomes, Year 8 pupils should, for example:

# Find the outcome of a given percentage increase or decrease.

#### Understand that:

- If something increases by 100%, it doubles.
- If something increases by 500%, it increases by five times itself, and is then six times its original size.
- A 100% decrease leaves zero.
- An increase of 15% will result in 115%, and 115% is equivalent to 1.15.
- A decrease of 15% will result in 85%, and 85% is equivalent to 0.85.
- An increase of 10% followed by a further increase of 10% is not equivalent to an increase of 20%.

## For example:

 An increase of 15% on an original cost of £12 gives a new price of

 $£12 \times 1.15 = £13.80$ 

or

15% of £12 = £1.80 £12 + £1.80 = £13.80

 A decrease of 15% on the original cost of £12 gives a new price of

 $£12 \times 0.85 = £10.20$ 

or

15% of £12 = £1.80 £12 - £1.80 = £10.20

#### Investigate problems such as:

- I can buy a bicycle for one cash payment of £119, or pay a deposit of 20% and then six equal monthly payments of £17.
   How much extra will I pay in the second method?
- A price is increased by 10% in November to a new price. In the January sales the new price is reduced by 10%. Is the January sale price more, less or the same as the price was in October? Justify your answer.
- At the end of a dinner the waiter added VAT of 17.5% and then a 12.5% service charge. The customer argued that the service charge should have been calculated first.

Who was correct?

Give mathematical reasons for your answer.

Link to enlargement and scale (pages 212–17), and area and volume (pages 234–41).

As outcomes, Year 9 pupils should, for example:

Use percentage changes to solve problems, choosing the correct numbers to take as 100%, or as a whole.

#### For example:

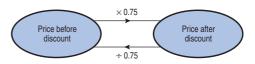
There was a 25% discount in a sale.
 A boy paid £30 for a pair of jeans in the sale.
 What was the original price of the jeans?

### Using a unitary method

£30 represents 75%.  $£30 \div 75$  represents 1%.  $£30 \div 75 \times 100$  represents 100%.

### Using inverse operations

Let p be the original price.  $p \times 0.75 = 30$ , so  $p = 30 \div 0.75 = 40$ 



An unstretched metal spring is 20 cm long.
 It is stretched to a length of 27cm.
 Find the percentage change in its length.

The increase is  $\frac{7}{20} = \frac{35}{100}$  or 35%.

#### Solve problems such as:

- A jacket is on sale at £45, which is 85% of its original price. What was its original price?
- I bought a fridge freezer in a sale and saved £49. The label said that it was a '20% reduction'. What was the original price of the fridge freezer?
- A stereo system has been reduced from £320 to £272. What is the percentage reduction?
- The number of people going to a cinema increased from 52 000 in 1998 to 71500 in 2001.
   Calculate the percentage increase in the number of people going to the cinema from 1998 to 2001.
- 12 500 people visited a museum in 2000.
  This was an increase of 25% on 1999.
  How many visitors were there in 1999?
- When heated, a metal bar increases in length from 1.25 m to 1.262m. Calculate the percentage increase correct to one decimal place.
- A woman deposits £75 in a bank with an annual compound interest rate of 6%. How much will she have at the end of 3 years? (The calculation 75 x (1.06)³ gives the new amount.)

Link to proportionality (pages 78–9), enlargement and scale (page 212–17), and area and volume (pages 234–41).

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